

## Chapter 10. Considerations for Statistical Analysis

### Abstract

This chapter provides a high level overview of statistical analysis considerations for observational comparative effectiveness research (CER). Descriptive and univariate analyses can be used to assess imbalances between treatment groups and identify covariates associated with exposure and/or the study outcome. Traditional strategies to adjust for confounding during the analysis include linear and logistic multivariable regression models. The appropriate analytic technique is dictated by the characteristics of the study outcome, exposure of interest, study covariates, and the underlying assumptions underlying the statistical model. Increasingly common in CER is the use of propensity scores, which assign a probability of receiving treatment conditional on observed covariates. Propensity scores are appropriate when adjusting for large numbers of covariates and are particularly favorable in studies having a common exposure and rare outcome(s). Disease risk scores estimate the probability or rate of disease occurrence as a function of the covariates and are preferred in studies with a common outcome and rare exposure(s). Instrumental variables, which are measures that are causally related to exposure but only affect the outcome through the treatment, offer an alternative to analytic strategies that have incomplete information on potential unmeasured confounders. Missing data in CER studies is not uncommon and it is important to characterize the patterns of missingness in order to account for missing data in the analysis. In addition, time-varying exposures and covariates should be accounted for to avoid bias. The chapter concludes with a checklist including guidance and key considerations for developing a statistical analysis section of an observational CER protocol or proposal.

### Introduction

Comparative effectiveness research utilizing observational data requires careful and often complex analytic strategies to adjust for confounding. This can include standard analytic strategies, such as traditional multivariable regression techniques, as well as newer, more sophisticated methodologies, such as propensity score matching and instrumental variable analysis. This chapter covers data analysis strategies from simple descriptive statistics to more complex methodologies. Also covered are important considerations such as handling missing data and analyzing time-varying exposures and covariates.

While this chapter provides a high level summary of considerations and issues for statistical analysis in observational CER, it is not intended to be a comprehensive treatment of considerations and approaches. We encourage the reader to explore topics more fully by referring to the references provided.

### Descriptive Statistics/Unadjusted Analyses

Appropriate descriptive statistics and graphical displays for different types of data have been presented in numerous textbooks.<sup>1</sup> This includes measures of range, dispersion, and central tendency for continuous variables, n and percent for categorical variables, and plots for evaluating data distributions. For comparative effectiveness research (CER), it is important to consider useful and informative applications of these descriptive statistics. For instance, for a cohort study, describing study covariates stratified by exposure levels provides a useful means to

assess imbalances in these measures. For a propensity matched-pairs dataset, summarizing study covariates by exposure group aids in detecting residual imbalances.

Univariate or unadjusted hypothesis testing, such as two-sample t-tests, can be conducted to identify covariates associated with the exposure and/or the study outcome. Since CER studies will need to consider potential confounding from a large number of study covariates, the descriptive statistics should provide a broad picture of the characteristics of the study subjects.

## Adjusted Analyses

### Traditional Multivariable Regression

Regression analysis is often used to control for potential confounding variables in the estimation of treatment effects.<sup>2</sup> In general, control is made for pre-treatment variables that are related to both the treatment of interest and the outcome of interest. Variables that are potentially on the pathway from treatment to outcome are not controlled for as control for such intermediate variables could block some of the effect of the treatment on the outcome. See chapter 7 (Covariate Selection) for further discussion. Traditional multiple regression, in which one uses regression models to directly adjust for potential confounders and effect modification, has long been used in observational studies and can be applied in CER. When applying regression modeling, careful attention must be paid to ensure corresponding model assumptions are met.<sup>3</sup> For instance, for logistic regression, as long as the number of outcome events per covariate included in the regression model is sufficient (e.g., rule of thumb is 10 or more) and the exposure of interest is not infrequent, traditional multiple regression is a reasonable strategy and could be considered the primary analysis.<sup>4,5</sup> However, when this is not the situation, other options should be considered.

When there are many covariates, one approach has been to develop more parsimonious models using methods such as stepwise regression. However, this may involve subjective decisions such as the type of variable selection procedure, whether to base selection upon p-values or change in exposure parameter estimates, and numeric cutoffs (e.g.,  $p=0.05$ , 0.10, 0.20) for variable inclusion and retention in the model. For covariates that confer relatively modest increases in disease risk, some variable selection procedures, such as stepwise regression, may exclude important covariates from the final model.

Furthermore, stepwise regression has limitations that can lead to underestimation of standard errors for exposure estimates.<sup>6</sup> Other analytical strategies which have become more common in recent years include using summary variables, such as propensity scores and disease risk scores, which are described below. Propensity scores often perform better than logistic regression when the outcome is relatively rare (e.g., fewer than 10 events per covariate as noted above), whereas logistic regression tends to perform better than propensity score analysis when the outcome is common but the exposure is rare.<sup>7</sup>

### Choice of Regression Modeling Approach

The forms of the study outcome, exposure of interest, and study covariates will determine the regression model to be used. For independent, non-time-varying exposures and study covariates, generalized linear models (GLM's) such as linear or logistic regression can be used. If the study

outcome is binary with fixed followup and is rare, Poisson regression with robust standard errors can be used to estimate relative risks and get correct confidence intervals.<sup>8,9</sup>

In CER studies in which data are correlated, regression models should be specified that take this correlation into account. Examples of correlated data include repeated measures on study subjects over time, patients selected within hospitals across many hospitals, and matched study designs. There are a number of analysis options that can be considered, which depend on the study question and particulars of the study design. Repeated measures per study subject can be collapsed to a single summary measure per subject. Generalized estimating equations (GEE) are a frequently-used approach to account for correlated data. Random effects models are another suitable analytical approach to handle repeated measures data. Approaches for such longitudinal data are described in detail in a number of textbooks.<sup>10,11</sup> For matched study designs (e.g., case-controlled designs), models such as conditional logistic regression may be considered.

Time-to-event data with variable follow-up and censoring of study outcomes are commonly investigated in CER studies. Cox proportional hazards regression is a common methodology for such studies. In particular, this approach can easily handle exposures and study covariates whose values vary over time as described in detail below. When time-varying covariates are affected by time-varying treatment, marginal structural models (described below) may be required. A number of excellent textbooks describe analyzing time-to-event data.<sup>12,13</sup>

A high-level overview of modeling approaches in relation to the nature of the outcome measure and followup assessments is shown in Table 10.1.

**Table 10.1. Summary of Modeling Approaches as a Function of Structure of Outcome Measure and Followup Assessments**

Number of follow-up measures and time intervals				
	Single measure		Repeated measure, fixed intervals	Repeated measure, variable intervals
Outcome measure	<i>No clustering</i>	<i>Clustering (e.g., multi-site study)</i>		
Dichotomous	Logistic regression	Multilevel (mixed) logistic regression, GLMM, GEE, conditional logistic regression	Repeated measures ANOVA (MANOVA), GLMM, GEE	GLMM, GEE
Continuous	Linear regression	Multilevel (mixed) linear regression, GLMM, GEE	Repeated measures ANOVA (MANOVA), GLMM, GEE	GLMM, GEE
Time to event	Cox proportional hazards regression	Variance-adjusted Cox model or shared frailty model		
Time to event	Poisson regression	Multilevel (mixed)		

Number of follow-up measures and time intervals			
(aggregate or count data)		Poisson regression	

NOTE: This high level summary provides suggestions for selection of a regression modeling approach based on consideration of the outcome measure and nature of the followup measures or assessments. Many of these methods allow time-varying exposures and covariates to be incorporated in the model. Time-varying **confounding** may require use of IPTW/marginal structural model techniques.

### Model Assumptions

All analytic techniques, including regression, have underlying assumptions. It is important to be aware of those assumptions and to assess them. Otherwise, there are risks with regards to interpretation of study findings. These assumptions and diagnostics are specific to the regression technique being used and will not be listed here. These are covered in numerous textbooks depending on the methods being used. For example, if Cox proportional hazards regression is used, then the proportional hazards assumption should be assessed. If this assumption is questionable, then alternatives, such as time-dependent covariates, may need to be considered.

### Propensity Scores

Propensity scores are an increasingly common analytic strategy for adjusting for large numbers of covariates in CER. The use of the propensity score for confounding control was proposed by Rosenbaum and Rubin.<sup>14</sup> The propensity score is defined as the probability of receiving treatment (or exposure) conditional on observed covariates and is typically estimated from regression models, such as a logistic regression of the treatment conditional on the covariates. Rosenbaum and Rubin showed that if adjustment for the original set of covariates suffices to control for confounding then adjustment for just the propensity score also would suffice as well. This strategy is particularly favorable in studies having a common exposure and rare outcome or possibly multiple outcomes.<sup>7</sup> Propensity scores can be used in sub-classification or stratification,<sup>15</sup> matching,<sup>16</sup> and weighting,<sup>17</sup> and further adjustment can be done using regression adjustment.<sup>18</sup> Stürmer and colleagues provide a review of the application of propensity scores.<sup>19</sup>

If adjustment using the propensity score is used, balance in study covariates between exposure groups should be carefully assessed. This can include, but is not limited to, testing for differences in study covariates by exposure group after adjusting for propensity score. Another common assessment of the propensity score is to visually examine the propensity score distributions across exposure groups. It has been demonstrated that if there is poor overlap in these distributions, there is a risk of biased exposure estimates when adjusting for the propensity score in a regression model.<sup>20</sup> One remedy for this is to restrict the cohort to subjects whose propensity score overlaps across all exposure groups.<sup>21,22</sup>

Matching on propensity score offers several advantages when feasible. Matching subjects across exposure groups on propensity score ensures, through restriction, that there will be good overlap in the propensity score distributions. In addition, summarizing subject characteristics by exposure groups in a propensity-matched design is akin to summarizing subject characteristics in a clinical trial to assessing balance in study covariates. However, in a propensity-matched design, one can only ensure that measured covariates are being balanced. The consequences of unmeasured confounding can be assessed using sensitivity analysis. See chapter 11 for further details. Matching techniques for causal effects are described in detail in Rubin<sup>23</sup> and best

practices for constructing a matched control group are provided by Stuart and Rubin.<sup>24</sup> Care must be taken when estimating standard errors for causal effects when using matching,<sup>25,26</sup> though software is now available that makes this task easier.<sup>27</sup>

A trade-off between using regression adjustment on the full cohort and a propensity-matched design is that in the former there still may be imbalances in study covariates and in the latter sample size may be reduced to the extent that some of subjects are unable to be matched. Connors and colleagues<sup>28</sup> used both analytic strategies in a cohort study of the effectiveness of right heart catheterization and reported similar findings from both analyses. Use of multiple analytic strategies as a form of sensitivity analysis may serve as a useful approach drawing from the strengths of both strategies.

Brookhart and colleagues<sup>29</sup> investigated variable selection approaches and recommend that covariates to be included in the propensity score model either be true confounders or at least related to the outcome; including covariates related only to the exposure, which increase the variance of the exposure estimate.

### Disease Risk Scores

The disease risk score (DRS) is an alternative approach to the propensity score.<sup>30,31</sup> Like the propensity score, it is a summary measure derived from the observed values of the covariates. However, the DRS estimates the probability or rate of disease occurrence as a function of the covariates. The DRS may be estimated in two ways. First, it can be calculated as a "full-cohort" DRS, which is the *multivariate confounder score* originally proposed by Miettinen (1976).<sup>32</sup> This score was constructed from a regression model relating the study outcome to the exposure of interest and the covariates for the entire study population. The score was then computed as the fitted value from that regression model for each study subject, setting the exposure status to non-exposure. The subjects were then grouped into strata according to the score and a stratified estimate of the exposure effect was calculated. The DRS also may be estimated as an "unexposed-only" DRS, from a regression model fit only for the unexposed population, with the fitted values then computed for the entire cohort.

The DRS is particularly favorable in studies having a common outcome and rare exposure or possibly multiple exposures. The DRS is useful for summarizing disease risk and assessing effect modification by disease risk. Ray and colleagues<sup>33</sup> reported effect modification by cardiovascular disease risk, derived and summarized using DRS, in a study of antipsychotics and sudden cardiac death. Also, in the presence of a multilevel exposure in which some of the levels are infrequent, the DRS may be a good alternative to propensity scores.

### Instrumental Variables

A limitation of study designs and analytic strategies, including traditional multiple regression, propensity scores, and disease risk scores in CER studies, is incomplete information on potential unmeasured confounders. An alternative approach to estimate causal effects, other than confounding/covariate control, is the use of instrumental variables.<sup>34</sup> An "instrument" is a measure that is causally related to exposure but only affects the outcome through the treatment and is also unrelated to the confounders of the treatment-outcome relationship. With an instrument, even if there is unmeasured confounding of the treatment-outcome relationship, the

effect of the instrument on the treatment, and the effect of the instrument on the outcome can together be used to essentially back out the effect of the treatment on the outcome. A difficulty of this approach is identifying a high-quality instrument.

An instrument must be unrelated to the confounders of the treatment and the outcome; otherwise instrumental variable analyses can result in biases. An instrument must also not affect the outcome except through the treatment. This assumption is generally referred to as the ‘exclusion restriction.’ Violations of this exclusion restriction can likewise result in biases. Finally, the instrument must be related to the treatment of interest. If the association between the instrument and the treatment is weak, the instrument is referred to as a ‘weak instrument.’ Finite-sample properties of estimators using weak instruments are often poor, and weak instruments moreover tend to amplify any other biases that may be present.<sup>35,36,37,38</sup>

Two-stage least squares techniques are often employed when using instrumental variables, though with a binary treatment, ratio estimators are also common.<sup>34</sup> For estimates to be causally interpretable, often a monotonicity assumption must also be imposed that the effect of instrument on the treatment only operates in one direction (e.g., it is causative or neutral for all individuals). Assumptions of homogeneous treatment effects across individuals are also an assumption that is commonly employed to obtain causally interpretable estimates. When homogeneity assumptions are not employed, the resulting causal effect estimate is generally only applicable for certain subpopulations consisting of those individuals for whom the instrument is able to change the treatment status.<sup>34</sup> Such effects are sometimes referred to as “local average treatment effects”. When the treatment is not binary, interpretation of the relevant subpopulation becomes more complex.<sup>39</sup> Moreover, when two-stage least squares procedures are applied to binary rather than continuous outcomes, other statistical biases can arise.<sup>40</sup>

Brookhart and colleagues<sup>41</sup> applied this approach in a study of COX-2 inhibitors with nonselective, nonsteroidal antiinflammatory drugs (NSAIDs) on gastrointestinal complications. Their instrument was the prescribing physician’s preference for a COX-2 inhibitor relative to an NSAID. The results of the instrumental variable analysis were statistically similar to results from two clinical trials, which was contrary to the traditional multiple regression analysis that was also conducted.

Schneeweiss and colleagues<sup>42</sup> examined aprotinin during coronary-artery bypass grafting (CABG) and risk of death in which their primary analysis was a traditional multiple regression. In addition to the primary analysis, they also conducted a propensity score matched-pairs analysis as well as an instrumental variable analysis. All three analyses had similar findings. This methodology of employing more than one analytical approach may be worth consideration since the propensity score matching does not rely on the exclusion restriction and other instrumental variable assumptions, whereas instrumental variable analysis circumvents the biases introduced by unmeasured confounders, provided a good instrument is identified. When results differ, careful attention needs to be given to what set of assumptions are more plausible.

### Missing Data Considerations

It is not uncommon to have missing data in CER. The extent of missing data and its potential impact on the analysis needs to be considered. Before proceeding with the primary analyses, it is

important to characterize the patterns of missingness using exploratory data analyses. This can provide insights into how to handle the missing data in the primary analysis.

For the primary analysis, a common analytical approach is to just analyze those subjects who have no missing data, called a complete-case analysis. However, an initial limitation with this is that sample size is reduced, which affects efficiency even if data are missing completely at random. If subjects with missing data differ from subjects with complete data, then exposure estimates may be biased. For example, suppose blood pressure is a potential confounder, and it is missing in very ill subjects. Then excluding these subjects can bias the exposure estimate.

Little and Rubin's textbook describes several analytic approaches for handling missing data.<sup>43</sup> One common approach to filling in missing data when they are "missing completely at random" or "missing at random" is imputation, which they describe in detail. In Chapter 3 of Harrell's textbook, he describes missing data and imputation and also provides some guidelines for handling such data.<sup>44</sup> Inverse probability weighting techniques, described below, can also be employed to address issues of missing data.

### Time-Varying Exposures/Covariates

In most CER studies, it is unrealistic to assume that exposures and covariates remain fixed throughout followup. Consider, for example, HIV patients who may be treated by anti-retroviral therapy. The use of anti-retroviral therapy may change over time and decisions about therapy may in part be based on CD4 count levels, which also vary over time. As another illustration, consider a study of whether or not proton pump inhibitors (PPIs) prevent clopidogrel-related gastroduodenal bleeding, and warfarin may be started during followup. Should one adjust for this important potential confounder? Failure to account for the time-varying status of such exposures and confounders (i.e., fix everyone's exposure status at baseline) may severely bias study findings.

As noted above, for time-to-event study outcomes, time-dependent Cox regression models can be used to account for time-varying exposures and covariates. However, difficult issues arise when both the treatment and confounding variables vary over time. In the HIV example, CD4 count may be affected by prior therapy decisions, but CD4 count levels may themselves go on to alter subsequent therapy decisions and the final survival outcome. In examining the effects of time-varying treatment, a decision must be made as to whether to control for CD4 count. A difficulty arises in that CD4 count is both a confounding variable (for subsequent therapy and final survival) and also an intermediate variable (for the effect of prior treatment). Thus control for CD4 count in a time-varying Cox model could potentially lead to bias because it is an intermediate variable and could thus block some of the effect of treatment; but failure to control for CD4 count in the model will result in confounding and thus bias for the effect of subsequent treatment. Both analyses are biased. Such problems arise whenever a variable is simultaneously on the pathway from prior treatment and also affects both subsequent treatment and the final outcome.

These difficulties can be addressed by using inverse-probability-of-treatment weighting,<sup>45</sup> rather than regression adjustment, for confounding control. These inverse-probability-of-treatment weighting (IPTW) techniques are used to estimate the parameters of what is often called a

marginal structural model, which is a model for expected counterfactual outcomes. The marginal structural model / IPTW approach is essentially a generalization of propensity score weighting to the time-varying treatment context. The IPTW technique assumes that at each treatment decision, the effect of treatment on the outcome is unconfounded given the past covariate and treatment history. A similar weighting approach can also be used to account for censoring as well.<sup>45</sup> This marginal structural model / IPTW approach has been developed for binary and continuous outcomes,<sup>45</sup> time-to-event outcomes,<sup>46</sup> as well as for repeated measures data.<sup>47</sup>

Another consideration for time-varying exposures is accounting for exposure effect (e.g., medication use) after the subject stopped receiving that exposure. One approach is to create another exposure level that is a carryover of a biologically plausible number of days after exposure use has ended and incorporate it as a time-varying exposure level in the analysis. Another approach is an intent-to-treat analysis in which exposure status (e.g., treatment initiation) is assumed throughout followup. Cadarette and colleagues (2008) used this approach in a study of fracture risk.<sup>48</sup> The motivation was that treatment adherence may be low and accounting for on-treatment status may result in information bias.

### **Conclusion**

This chapter provides a brief overview of statistical methods, and offers suggestions and recommendations to address the complex challenges of analyzing data from observational CER studies. Both traditional approaches such as multivariable regression and novel but established methods such as propensity scores and instrumental variable approaches may be suitable to address specific data structures and under certain assumptions. Thoughtful application of these approaches can help the investigator improve causal inference.

### Checklist: Guidance and Key Considerations for Developing a Statistical Analysis Section of an Observational CER Protocol or Proposal

Guidance	Key Considerations	Check
Describe the key variables of interest with regard to factors that determine appropriate statistical analysis	<ul style="list-style-type: none"> <li>- Independent variables (when are they measured, fixed or time-varying; e.g., exposures, confounders, effect modifiers)</li> <li>- Dependent variables or outcomes (continuous or categorical, single or repeated measure, time to event)</li> <li>- State if there will be a “multi-level” analysis (e.g., looking at effects of both practice level and patient level characteristics on outcome)</li> </ul>	<input type="checkbox"/>
Propose descriptive analysis or graph according to treatment group	<ul style="list-style-type: none"> <li>- Should include the available numbers per group, n missing for all key covariates, distributions or graphs that are needed to decide if transformation of data is needed or determine an accurate functional form of the final model</li> <li>- Should include all potential confounders and effect modifiers to assess initial covariate balance by study group</li> </ul>	<input type="checkbox"/>
Propose the model that will be used for primary and secondary analysis objectives	<ul style="list-style-type: none"> <li>- Should take into account the design (independent vs. dependent observations, matched, repeated measurement, clustered); objectives, functional form of model, fixed/time-varying followup period, fixed and time-varying exposure and other covariates, assessment of effect modification/heterogeneity, type of outcome variables (categorical, ordinal, or continuous), censored data, and the degree of rarity of outcome and exposure</li> <li>- Should propose suitable approach for adjusting for confounding (e.g., Multiple regression model, propensity scores, IV [could be secondary or main analysis])</li> </ul>	<input type="checkbox"/>

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